

Claims:

1. A method of determining at least rotation and scale parameters of a transformation relating two images, said method comprising the steps of:
 - 5 forming a spatial domain representation of each of said images that is invariant to translation of said images;
performing correlation in the log-polar domain between said representations;
detecting a magnitude peak in said correlation; and
determining said rotation and scale parameters from the position of said
10 magnitude peak.
2. A method as claimed in claim 1 wherein the step of forming said representation of said images comprises the sub-steps of, for each said image:
 - 15 performing a Fourier transform of said image to form a Fourier transformed image;
performing a function on the magnitude component of said Fourier transformed image to form an altered Fourier transformed image, said function being commutative within a constant to rotation and scale; and
performing an inverse Fourier transform on said altered Fourier transformed
20 image to form said representation.
3. A method as claimed in claim 1 wherein the step of forming said representation of said images comprises the sub-steps of, for each said image:
 - 25 performing a Fourier transform of said image to form a Fourier transformed image;

performing a function on the magnitude component of said Fourier transformed image to form an altered Fourier magnitude image, said function being commutative within a constant to rotation and scale;

taking the second or higher derivatives of the phase component of said Fourier transformed image to form an altered Fourier phase image;

combining said altered Fourier magnitude and altered Fourier phase images to form an altered Fourier transformed image; and

performing an inverse Fourier transform on said altered Fourier transformed image to form said representation.

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4. A method as claimed in claim 3 wherein said altered Fourier phase image is formed by applying the Laplacian operator to said phase component of said Fourier transformed image.

15 5. A method as claimed in claim 3 or 4 wherein said altered Fourier magnitude and altered Fourier phase images are combined by using said altered Fourier magnitude image as a real part of said altered Fourier transformed image, and using said altered Fourier phase image as an imaginary part of said altered Fourier transformed image.

20 6. A method of determining at least rotation and scale parameters of a transformation relating two images, said method comprising the steps of:

forming a multi-channel function of each of said images by applying an operator to said images, said operator being commutative within a constant to rotation and scale;

forming a representation of each of said multi-channel functions that is invariant to translation of said multi-channel function;

performing correlation in the log-polar domain between said representations;

detecting a magnitude peak in said correlation; and

5 determining said rotation and scale parameters from the position of said magnitude peak.

7. A method as claimed in claim 6 wherein the step of forming said multi-channel functions comprises the sub-steps of, for each image:

10 convolving said image with a complex kernel function; and

multiplying said image with the result of the convolution step, wherein said complex kernel function has the Fourier transform of:

$$K(u, v) = \frac{u + iv}{|u + iv|}.$$

15 8. A method as claimed in claim 6 wherein the step of forming said multi-channel functions comprises the sub-steps of, for each image:

convolving said image with a complex kernel function; and

multiplying said image with the result of the convolution step, wherein said complex kernel function has the Fourier transform of:

20 $K'(u, v) = u + iv.$

9. A method as claimed in claim 6 wherein the step of forming said multi-channel functions comprises, for each image:

applying an energy operator to said image to form said multi-channel function,
where said energy operator is described by

$$E[I] = ID^2I - (DI)^2,$$

wherein D is the derivative operator.

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10. A method as claimed in claim 6 wherein the step of forming said multi-channel functions comprises, for each image:

applying a uni-modular energy operator to said image to form said multi-channel function, where said uni-modular energy operator is described by

$$E'[I] = ID'^2I - (D'I)^2,$$

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wherein D' is the uni-modular derivative operator.

11. A method as claimed in claim 9 or 10 wherein the step of forming said multi-channel functions comprises the further sub-step of:

15 normalising the result of the applying step.

12. A method as claimed in claim 9 or 10 wherein the step of forming said multi-channel functions comprises the further sub-step of:

multiplying said image with the result of the applying step.

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13. A method as claimed in claim 9 or 10 wherein the step of forming said multi-channel functions comprises the further sub-steps of:

normalising the result of the applying step; and

multiplying said image with the result of the normalising step.

14. A method as claimed in any one of claims claim 6 to 13 wherein said representations are in the spatial domain.

5 15. A method as claimed in any one of claims claim 1 to 14 wherein said correlation is the Fourier-Mellin correlation.

16. An apparatus for determining at least rotation and scale parameters of a transformation relating two images, said apparatus comprising:

10 means for forming a spatial domain representation of each of said images that is invariant to translation of said images;

means for performing correlation in the log-polar domain between said representations;

means for detecting a magnitude peak in said correlation; and

15 means for determining said rotation and scale parameters from the position of said magnitude peak.

17. An apparatus for determining at least rotation and scale parameters of a transformation relating two images, said apparatus comprising:

20 means for forming a multi-channel function of each of said images by applying an operator to said images, said operator being commutative within a constant to rotation and scale;

means for forming a representation of each of said multi-channel functions that is invariant to translation of said multi-channel function;

means for performing correlation in the log-polar domain between said representations;

means for detecting a magnitude peak in said correlation; and

means for determining said rotation and scale parameters from the position of
5 said magnitude peak.

18. A program stored on a memory medium for determining at least rotation and scale parameters of a transformation relating two images, said program comprising:

code for forming a spatial domain representation of each of said images that is
10 invariant to translation of said images;

code for performing correlation in the log-polar domain between said representations;

code for detecting a magnitude peak in said correlation; and

code for determining said rotation and scale parameters from the position of
15 said magnitude peak.

19. A program stored on a memory medium for determining at least rotation and scale parameters of a transformation relating two images, said program comprising:

code for forming a multi-channel function of each of said images by applying
20 an operator to said images, said operator being commutative within a constant to rotation and scale;

code for forming a representation of each of said multi-channel functions that is invariant to translation of said multi-channel function;

code for performing correlation in the log-polar domain between said
25 representations;

code for detecting a magnitude peak in said correlation; and

code for determining said rotation and scale parameters from the position of said magnitude peak.

- 5 20. A method of determining at least rotation and scale parameters of a transformation relating two images, said method being substantially as described herein with reference to the accompanying drawings.